NTHU MATH 2810, 2024



made by S.-W. Cheng (NTHU, Taiwan)

NTHU MATH 2810, 2024

proof (i) & (ii) holds by the definition of pmf.). 5-7
Actually, $f_{x}(x) = P(\{\omega \in \Omega \mid X(\omega) = x\})$	
$P_{\mathbf{x}}(\{\mathbf{x} \mathbf{f}_{\mathbf{x}}(\mathbf{x}) = 0\}) (\mathbf{i}\mathbf{v}) \text{ For } A \subset \mathbb{R} \text{ , let } A \cap \mathcal{X} = \{ \mathbf{x}_{1}^{\prime}, \mathbf{x}_{2}^{\prime}, \mathbf{x}_{3}^{\prime}, \cdots \}$	
= o, for $P_{X}(A) = P(\{\omega \in \Omega \mid X(\omega) \in A \cap \mathcal{X}\}) + P(\{\omega \in \Omega \mid X(\omega) \in A \cap \mathcal{X}^{c}\})$	ϕ
discrete r.v.'s $R(An \times) = \sum_{n=1}^{\infty} D(S_{n} \times O(n) - \gamma(n)) = \sum_{n=1}^{\infty} F(n') = \sum$	ア
$\frac{1}{100} \frac{1}{100} \frac{1}$	()
continuous (iii) follows (iv) by letting the A in (iv) be \mathcal{X} , then	
$\sum_{x \in \mathcal{X}} f_x(x) = P_x(\mathcal{X}) = P(\Omega) = 1.$	
check uniform Theorem. Any function f that satisfies (i), (ii), and (iii) for	
in LNp.3-18 some finite or countably infinite set χ is the pmf of some	
$\underline{\text{discrete}} \text{ random variable } \underline{X} : \Omega \rightarrow \mathbb{R} \neg \subset \mathbb{R}$	
proof. For given $X \& f$, let $\Omega = X \subset \mathbb{R}$.	
For any $A \subset X$, let $P(A) \equiv \sum_{x \in A} f(x)$. $(*)$	
Then, $(\Omega, \{A\}=2^{\Omega}, P)$ is a probability space (exercise	2)
Let $X: \Omega \rightarrow \mathbb{R}$ s.t. $X(\omega) = \omega$, $\forall \omega \in \Omega$.	·
Then, X is a discrete random variable with distribution.	Px,
and for any $x \in \mathbb{R}$, $by(*)$	
$f_{x}(x) = P_{x}(\{x\}) = P(\{x\}) \stackrel{!}{=} f(x)$	
■ Henceforth, we can <u>define</u> " <u>pmf</u> " as any <u>function</u> that satisfies (i), (ii), and (iii).). 5-8
• Henceforth, we can <u>define</u> " <u>pmf</u> " as any <u>function</u> that ignore the satisfies (i), (ii), and (iii). • We can specify a distribution by giving \mathcal{X} and f , subject to). 5-8
Henceforth, we can <u>define</u> " <u>pmf</u> " as any <u>function</u> that <u>satisfies (i), (ii), and (iii)</u> . <u>satisfies (i), (ii), and (iii)</u> . We can <u>specify a distribution</u> by giving $\underline{\mathcal{X}}$ and \underline{f} , <u>subject to</u> the three conditions (i), (ii), (iii).	o. 5-8
Henceforth, we can <u>define</u> " <u>pmf</u> " as any <u>function</u> that satisfies (i), (ii), and (iii). original probability space $(\Omega, \mathcal{F}, \mathbb{P})$). 5-8
Sort of ignore the original probability space (Ω, \mathcal{F}, P) \mathbb{Q} : Suppose that X and Y are two r.v.'s \mathbb{Q} is \mathbb{Q} is	5. 5-8
Sort of ignore the original probability space (Ω, \mathcal{F}, P) \mathbb{Q} : Suppose that X and Y are two $r.v.$'s defined on Ω with the same pmf. Is it $\mathbb{Q} \in \Omega^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{R}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{Q}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{Q}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{Q}^2$ $\mathbb{Q} = \mathbb{Q}^2$. Suppose that $X = M^2 + \mathbb{Q}^2$. Suppose \mathbb{Q}^2 is the maximum multiple of \mathbb{Q}^2. Suppose Q	2 ,
Sort of Sort of ignore the original probability space (Ω, \mathcal{F}, P) Check \neq in Me can specify a distribution by giving \mathcal{X} and f , subject to the three conditions (i), (ii), (iii). (Ω, \mathcal{F}, P) $(\Omega, $	2. 5-8
Henceforth, we can <u>define</u> " <u>pmf</u> " as any <u>function</u> that <u>satisfies (i), (ii), and (iii)</u> . We can <u>specify a distribution</u> by giving \mathcal{X} and \underline{f} , <u>subject to</u> the three <u>conditions (i), (ii), (iii)</u> . \mathcal{X} and \underline{f} , <u>subject to</u> the three <u>conditions (i), (ii), (iii)</u> . \mathcal{X} and \underline{f} , <u>subject to</u> the three <u>conditions (i), (ii), (iii)</u> . \mathcal{X} and \underline{f} , <u>subject to</u> the three <u>conditions (i), (ii), (iii)</u> . \mathcal{X} and \underline{f} , <u>subject to</u> the three <u>conditions (i), (ii), (iii)</u> . \mathcal{X} and \underline{f} , <u>subject to</u> the three <u>conditions (i), (ii), (iii)</u> . \mathcal{X} and \underline{f} , <u>subject to</u> \mathcal{X} and \underline{f}	2. 5-8
Henceforth, we can <u>define</u> " <u>pmf</u> " as any <u>function</u> that satisfies (i), (ii), and (iii). original probability We can <u>specify</u> a <u>distribution</u> by giving \mathcal{X} and f , <u>subject to</u> the three <u>conditions (i), (ii), (iii)</u> . \mathcal{X} and f , <u>subject to</u> the three <u>conditions (i), (ii), (iii)</u> . \mathcal{X} and f , <u>subject to</u> the three <u>conditions (i), (ii), (iii)</u> . \mathcal{X} and f , <u>subject to</u> the three <u>conditions (i), (ii), (iii)</u> . \mathcal{X} and f , <u>subject to</u> the three <u>conditions (i), (ii), (iii)</u> . \mathcal{X} and f , <u>subject to</u> the three <u>conditions (i), (ii), (iii)</u> . \mathcal{X} and f , <u>subject to</u> the three <u>conditions (i), (ii), (iii)</u> . \mathcal{X} and f , <u>subject to</u> the three <u>conditions (i), (ii), (iii)</u> . \mathcal{X} and f , <u>subject to</u> the three <u>conditions (i), (ii), (iii)</u> . \mathcal{X} and f , <u>subject to</u> \mathcal{X} and f , <u>subject to</u> \mathcal{X} and f , <u>subject to</u> \mathcal{X} and f . \mathcal{X} and f and	۵. 5-8 ≤ . €R
Henceforth, we can define "pmf" as any function that satisfies (i), (ii), and (iii). original probability space (Ω, \Im, P) Q: Suppose that X and Y are two r.v.'s defined on Ω with the same pmf. Is it Ans.No. always true that $X(\omega) = Y(\omega)$ for $\omega \in \Omega$? Definition: A function $F_X: \mathbb{R} \to \mathbb{R}$ is called the cumulative distribution function of a random variable X if $F_X(x) = P_X(X \le x), x \in \mathbb{R}$.	2. 5-8 ≤ . 2 €R ,∞
Sort of the satisfies (i), (ii), and (iii). Sort of the satisfies (i), (ii), and (iii). We can specify a distribution by giving \mathcal{X} and f , subject to the three conditions (i), (ii), (iii). (Ω, J, P) Q: Suppose that X and Y are two r.v.'s defined on Ω with the same pmf. Is it defined on Ω with the same pmf. Is it $\mathcal{X} = \mathcal{X} = \mathcal{X}$ Ans. No always true that $X(\omega) = Y(\omega)$ for $\omega \in \Omega$? Definition: A function $F_X: \mathbb{R} \to \mathbb{R}$ is called the cumulative distribution function of a random wratable X if $F_X(x) = P_X(X \le x), x \in \mathbb{R}$. (Note. The definition of cdf can be applied $(\mathcal{X} = \mathcal{X}) - \mathcal{X}$	2. 5-8 2. €R (∞))
Sort of Ignore the satisfies (i), (ii), and (iii). We can specify a distribution by giving \mathcal{X} and f , subject to the three conditions (i), (ii), (iii). Space (Ω, \mathcal{F}, P) Q: Suppose that X and Y are two r.v.'s defined on Ω with the same pmf. Is it Ans. No. always true that $X(\omega) = Y(\omega)$ for $\omega \in \Omega$? Definition: A function $F_X: \mathbb{R} \to \mathbb{R}$ is called the cumulative distribution function of a random variable X if $F_X(x) = P_X(X \le x), x \in \mathbb{R}$. (Note. The definition of cdf can be applied to arbitrary r.v.'s) espace on (as, x), yre (C, C, C, C, C) (C, C, C) (C,	2. 5-8 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
Henceforth, we can define "pmf" as any function that satisfies (i), (ii), and (iii). We can specify a distribution by giving \mathcal{X} and f , subject to the three conditions (i), (ii), (iii). $(\Omega, \mathfrak{F}, P)$ $(\Omega, \mathfrak{F}, F)$ $(\Omega, \mathfrak{F}, F)$ (Ω, \mathfrak{F}) (Ω, \mathfrak{F})	≥. 5-8 ≤. (2 (∞)) (2) (2) (2) (2) (2) (2) (2) (2) (2) (
Henceforth, we can define "pmf" as any function that satisfies (i), (ii), and (iii). We can specify a distribution by giving \mathcal{X} and f , subject to the three conditions (i), (ii), (iii). (Ω, \mathfrak{F}, P) \mathcal{O} : Suppose that X and Y are two r.v.'s defined on Ω with the same pmf. Is it $\mathcal{O} = \mathcal{O}(\Omega)$ for $\Omega \in \Omega$? $\mathcal{O} = \mathcal{O}(\Omega)$ for $\Omega = Y(\Omega)$ for $\Omega \in \Omega$? $\mathcal{O} = \mathcal{O}(\Omega)$ for $\Omega = Y(\Omega)$ for $\Omega = \Omega$? $\mathcal{O} = \mathcal{O}(\Omega)$ for $\Omega = Y(\Omega)$ for $\Omega = \Omega$? $\mathcal{O} = \mathcal{O}(\Omega)$ for $\Omega = Y(\Omega)$ for $\Omega = \Omega$? $\mathcal{O} = \mathcal{O}(\Omega)$? 	2. 5-8 ≤ . €R (∞)) sets,
Sort of ignore the satisfies (i), (ii), and (iii). We can specify a distribution by giving \mathcal{X} and f , subject to the three conditions (i), (ii), (iii). We can specify a distribution by giving \mathcal{X} and f , subject to the three conditions (i), (ii), (iii). $(\Omega, \mathfrak{F}, P)$ $(\Omega, \mathfrak{F}, F)$ $(\Omega, \mathfrak{F}, F)$ (Ω, \mathfrak{F}) (Ω, \mathfrak{F}) $(\Omega,$	2. 5-8 ≤ . € R (∞)) sets.
$\begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} $	5. 5-8 5. 5-8 5. 5-8 6 7 8 8 7 8

made by S.-W. Cheng (NTHU, Taiwan)